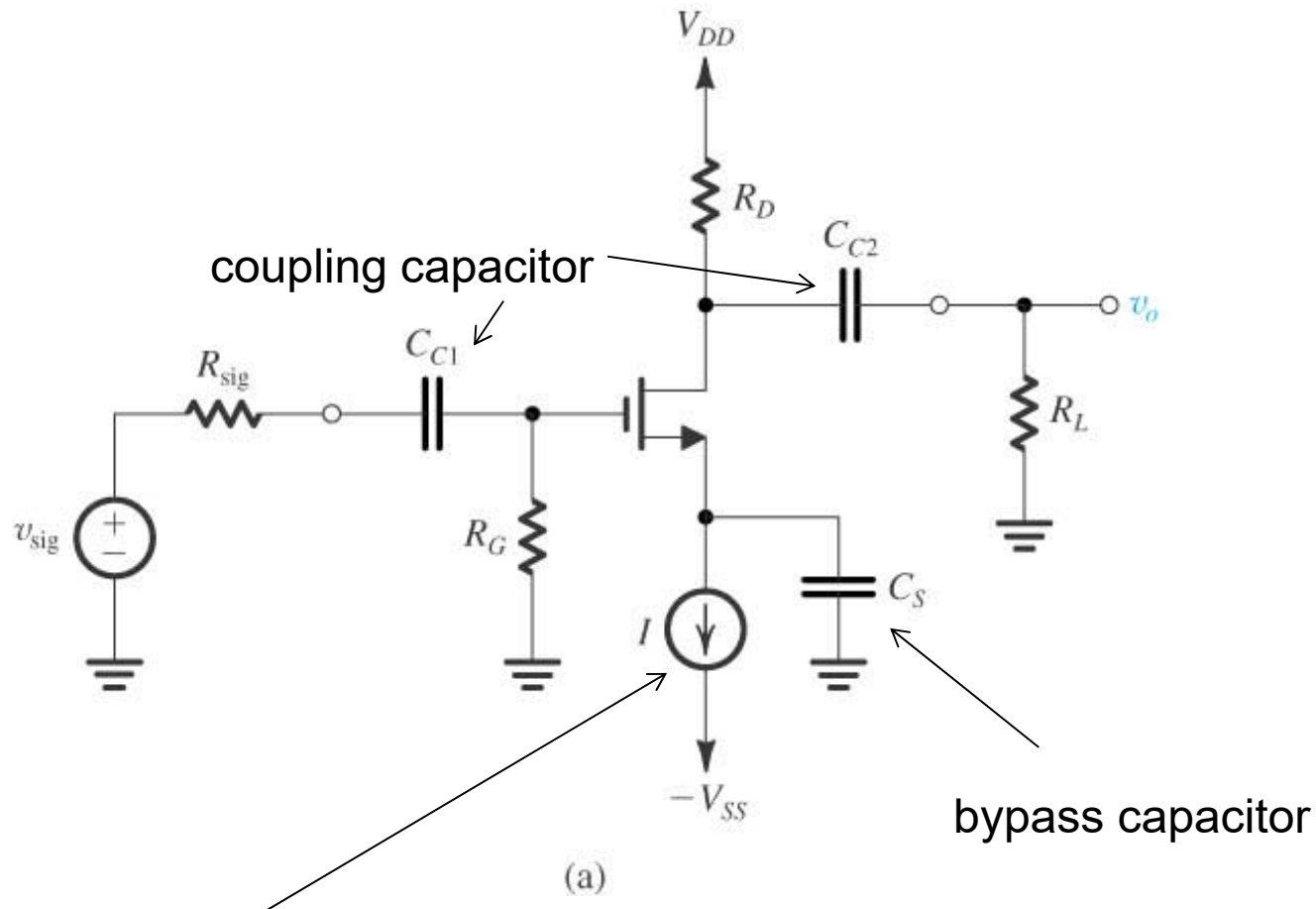


Single-Stage MOS Amplifiers

- ◆ Common Source Amplifier (biasing w/ current source)

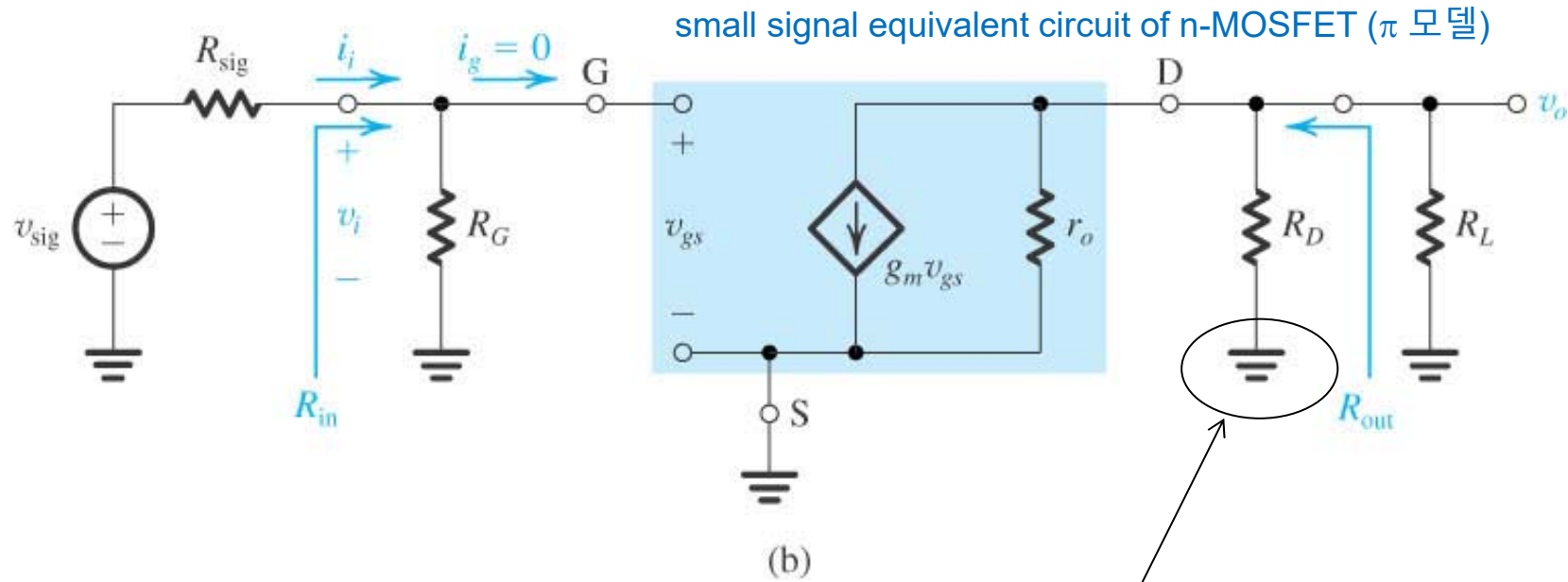


Biasing w/ current source

Single-Stage MOS Amplifiers

◆ Common Source Amplifier

$$g_m = \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}$$



Equivalent circuit of the amplifier for small-signal analysis.

DC 회로 상의 고정 전압은 소신호 회로 상에서는 **ground!**

DC bias 전류의 크기는 소신호 등가회로 모델 상에서 g_m 의 크기 결정.

$$i_g = 0$$

$$R_{in} = R_G$$

$$v_i = v_{sig} \frac{R_{in}}{R_{in} + R_{sig}} = v_{sig} \frac{R_G}{R_G + R_{sig}}$$

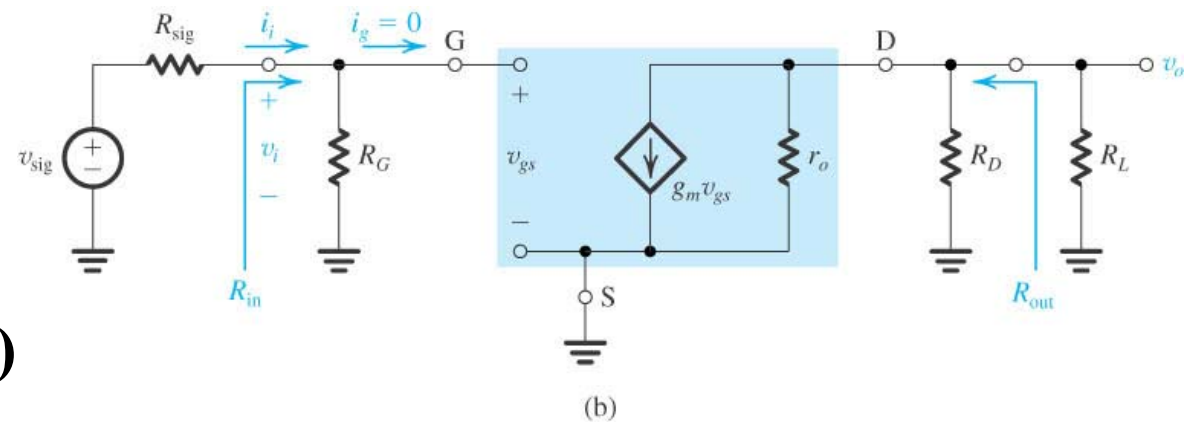
$$v_i \cong v_{sig}$$

$$v_{gs} = v_i$$

$$v_o = -g_m v_{gs} (r_o \parallel R_D \parallel R_L)$$

$$A_v = -g_m (r_o \parallel R_D \parallel R_L)$$

$$A_{vo} = -g_m (r_o \parallel R_D)$$



$$G_v = \frac{R_{in}}{R_{in} + R_{sig}} A_v$$

$$= \frac{R_G}{R_G + R_{sig}} g_m (r_o \parallel R_D \parallel R_L)$$

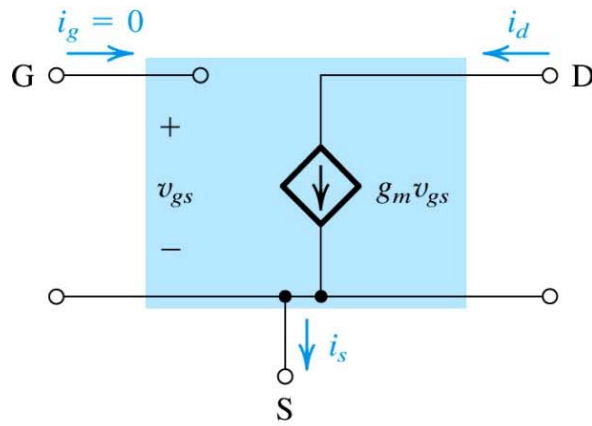
$$R_{out} = r_o \parallel R_D \quad (\text{by assuming } v_{sig} = 0)$$

CS 증폭기:

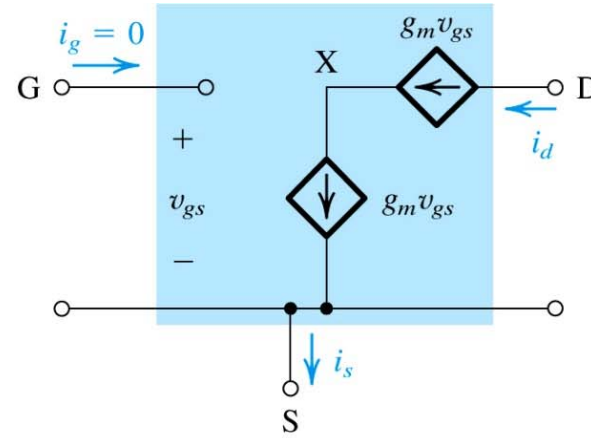
-매우 높은 입력 전압, 적당히 높은 전압 이득, 상대적으로 높은 출력 저항.

-일반적으로 다단 증폭기의 첫 번째 단으로 활용되며, 필요한 이득의 대부분을 얻는 데 가장 적합.

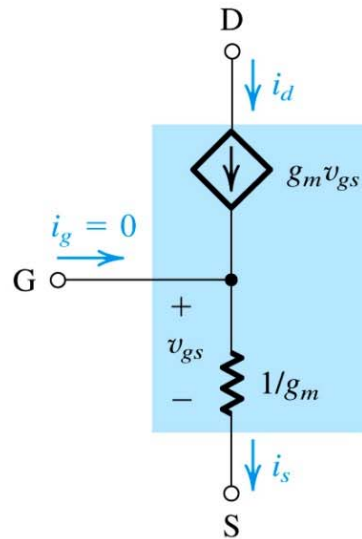
Small signal equivalent circuit of n-MOSFET (T 모델)



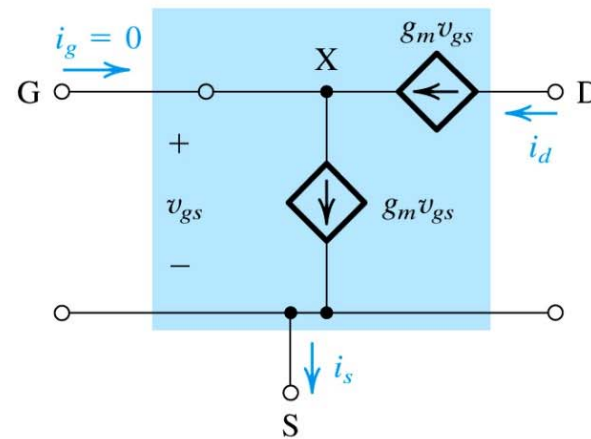
(a)



(b)



(d)



(c)

Small signal equivalent circuit of n-MOSFET (T 모델)

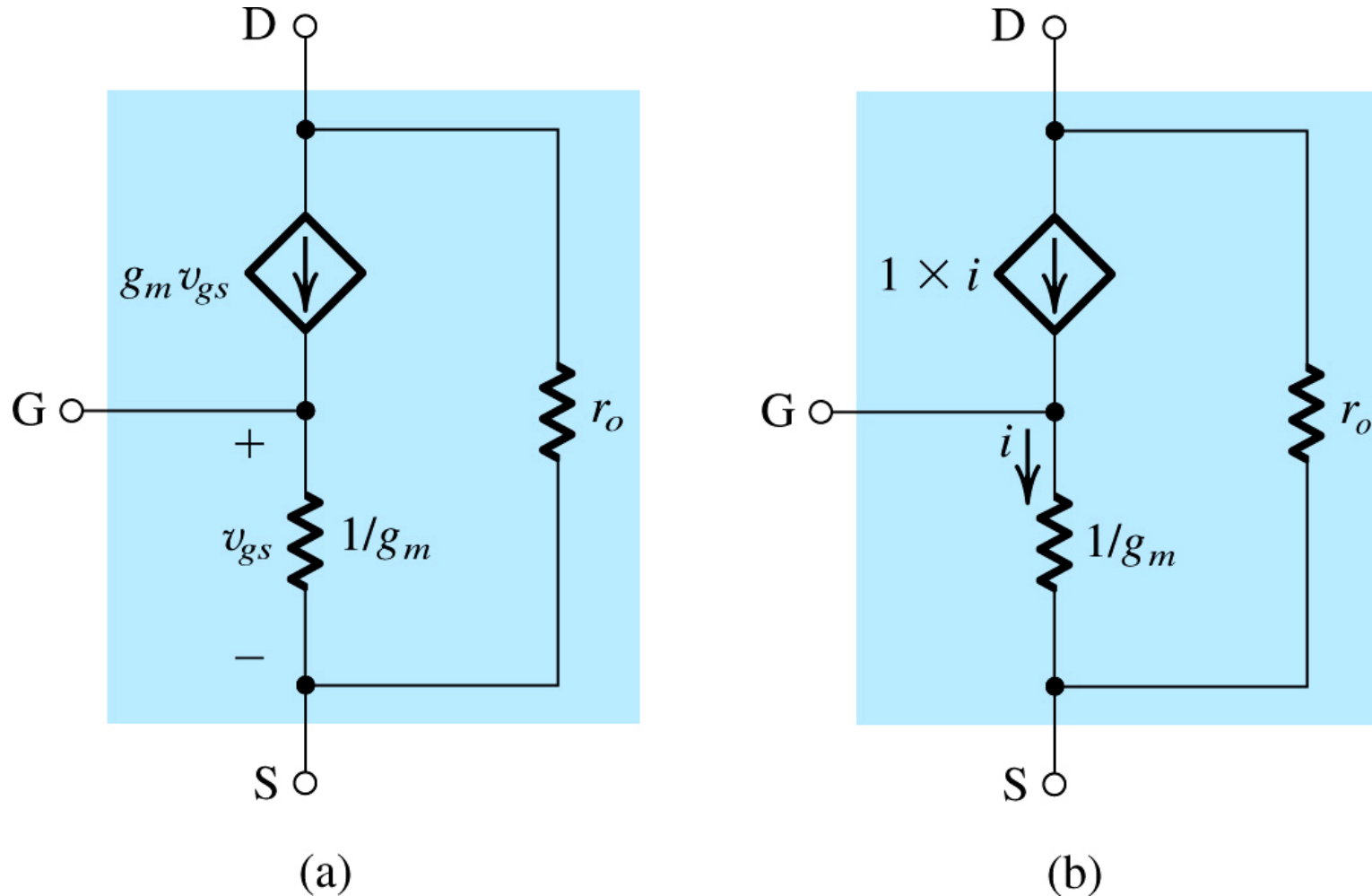
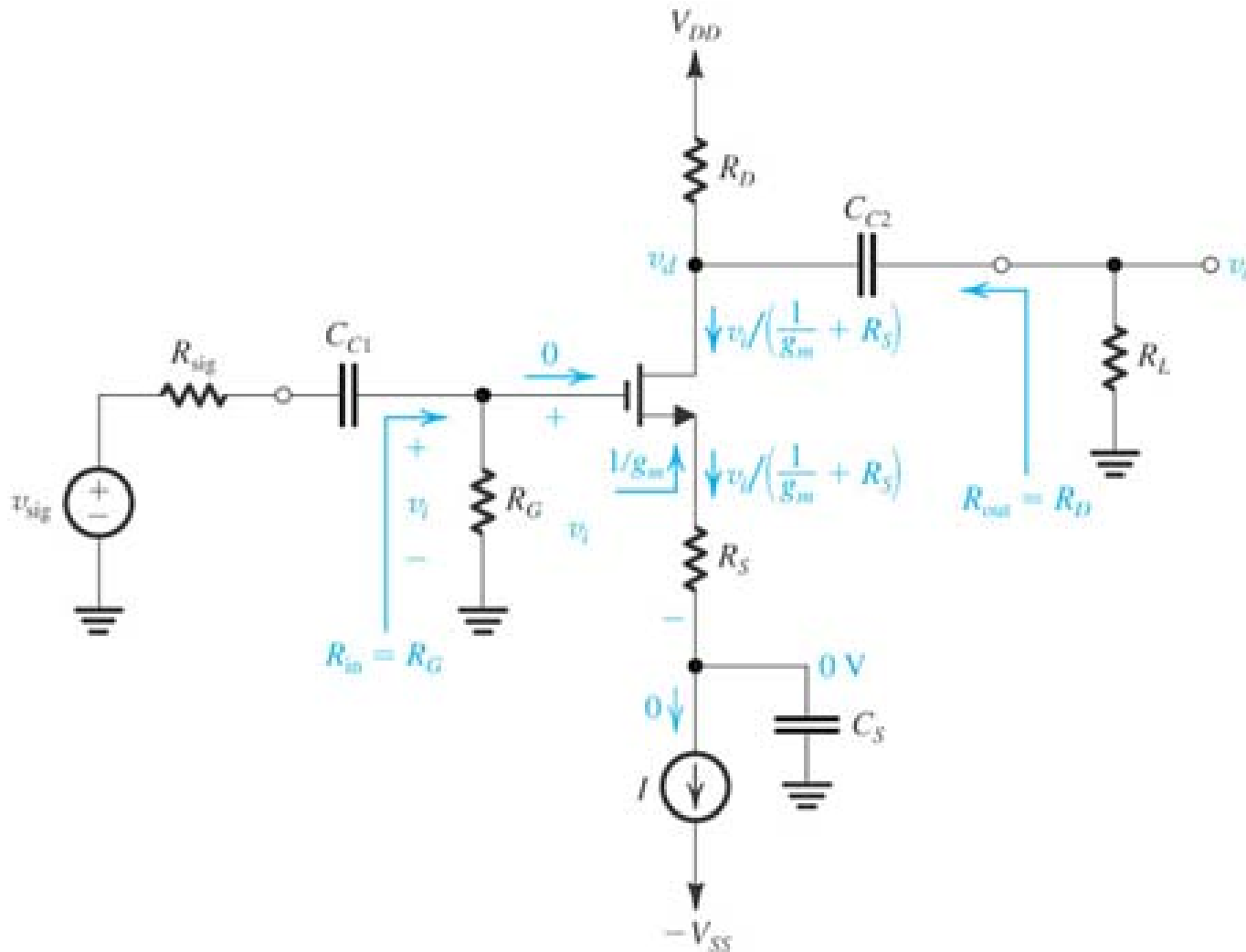
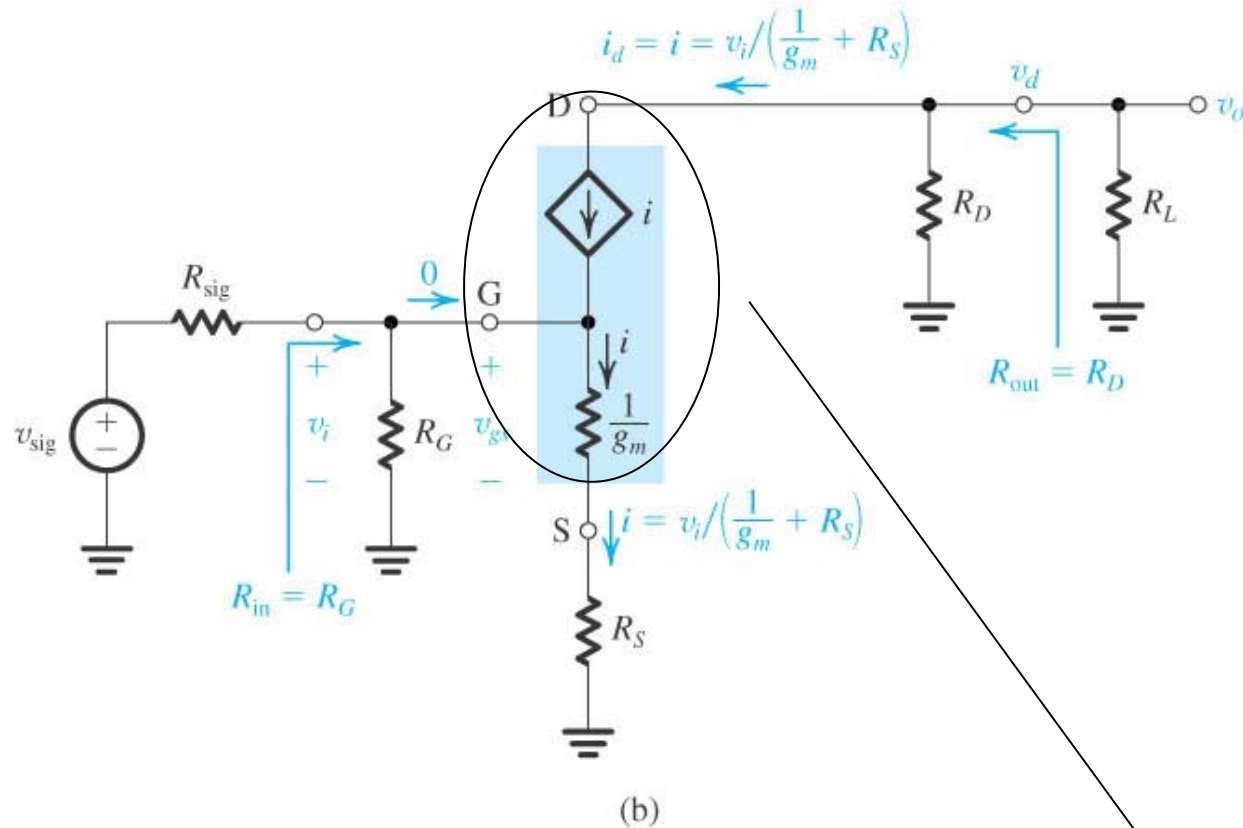


Figure 5.41 (a) The T model of the MOSFET augmented with the drain-to-source resistance r_o . (b) An alternative representation of the T model.

◆ Common Source Amplifier w/ source resistance



◆ Common Source Amplifier w/ source resistance



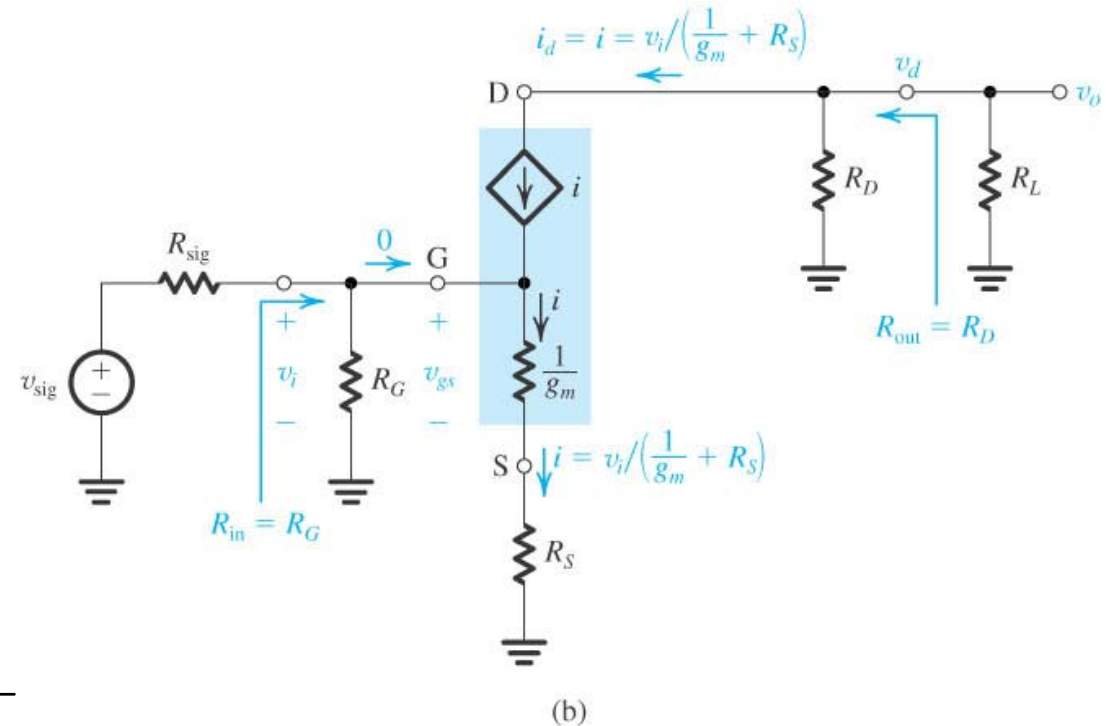
T model,
Source 단이 저항과 직렬 연결된 경우, 일반적으로 사용

$$R_{in} = R_i = R_G$$

$$v_i = v_{sig} \frac{R_G}{R_G + R_{sig}}$$

$$v_{gs} = v_i \frac{1}{\frac{1}{g_m} + R_S} = \frac{v_i}{1 + g_m R_S}$$

$$i_d = i = \frac{v_i}{\frac{1}{g_m} + R_S} = \frac{g_m v_i}{1 + g_m R_S}$$



We can reduce the input signal by increasing the magnitude of R_S

Bandwidth is increased. (next chapter)

Output resistance is decreased. (next chapter)

$$V_o = -i_d (R_D \parallel R_L)$$

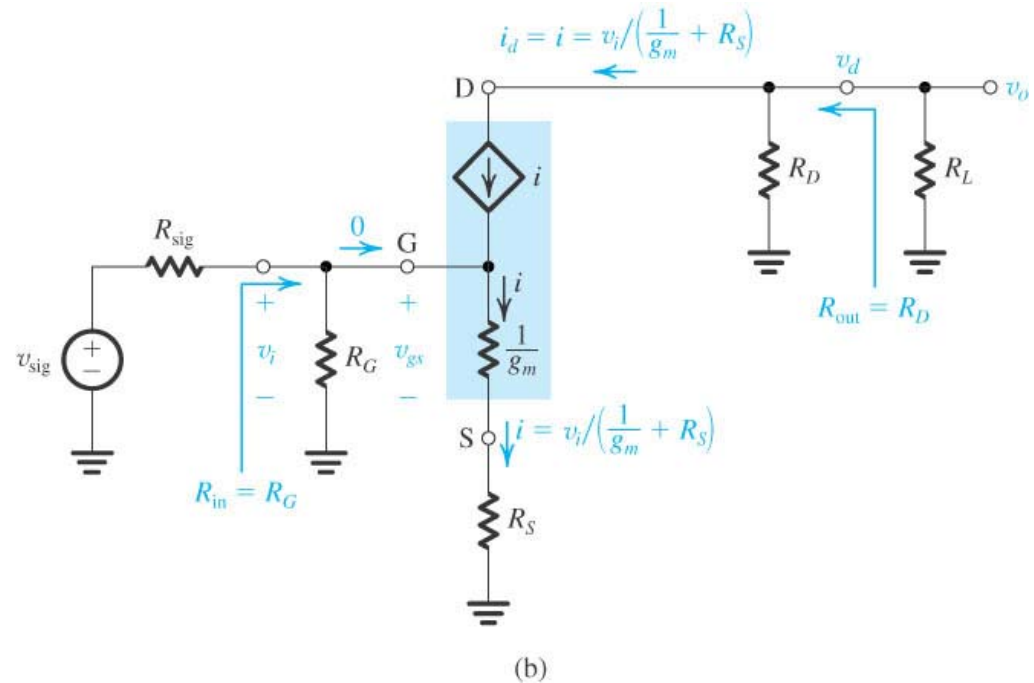
$$= -\frac{g_m (R_D \parallel R_L)}{1 + g_m R_S} v_i$$

$$A_v = -\frac{g_m (R_D \parallel R_L)}{1 + g_m R_S}$$

$$A_{vo} = -\frac{g_m R_D}{1 + g_m R_S}$$

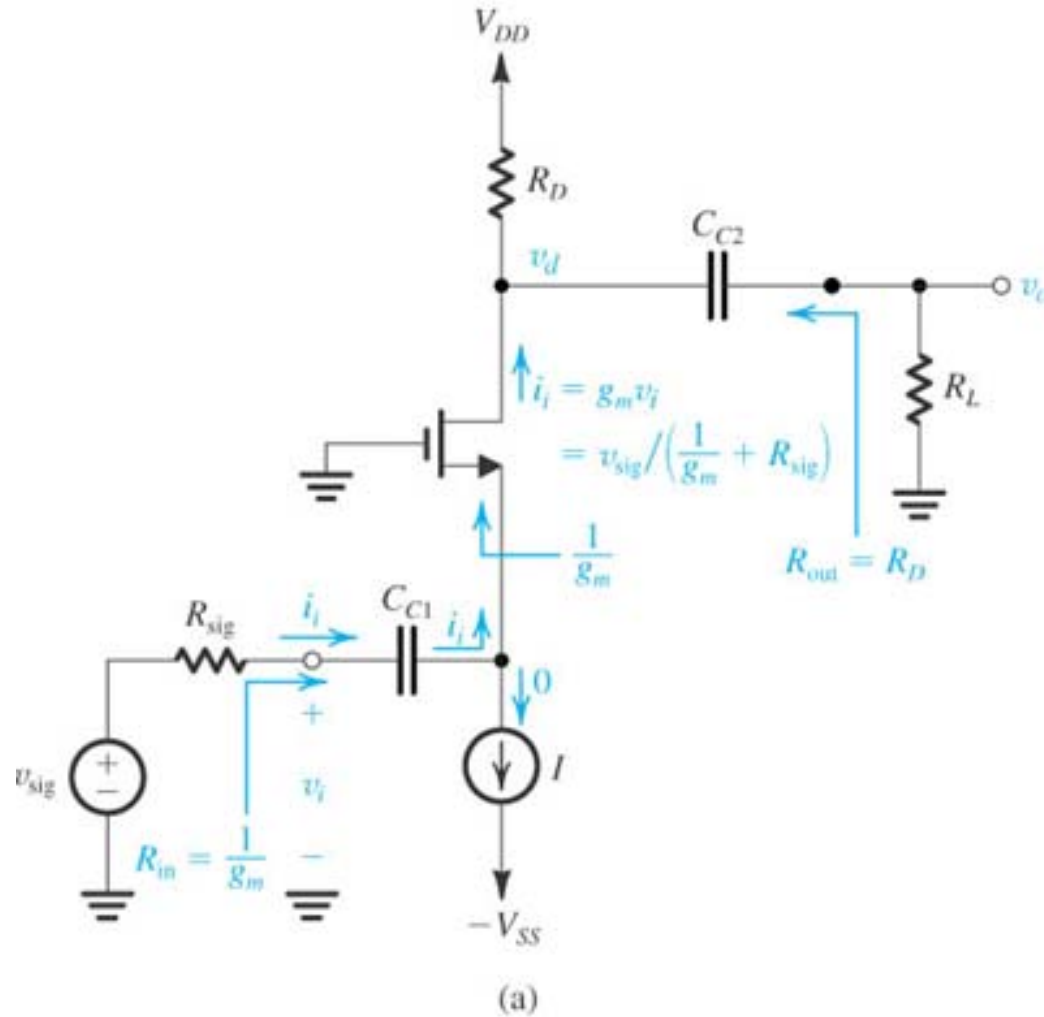
Voltage gain is reduced compared w/ CS without source resistance

$$G_v = \frac{R_G}{R_G + R_{sig}} \frac{g_m (R_D \parallel R_L)}{1 + g_m R_S}$$



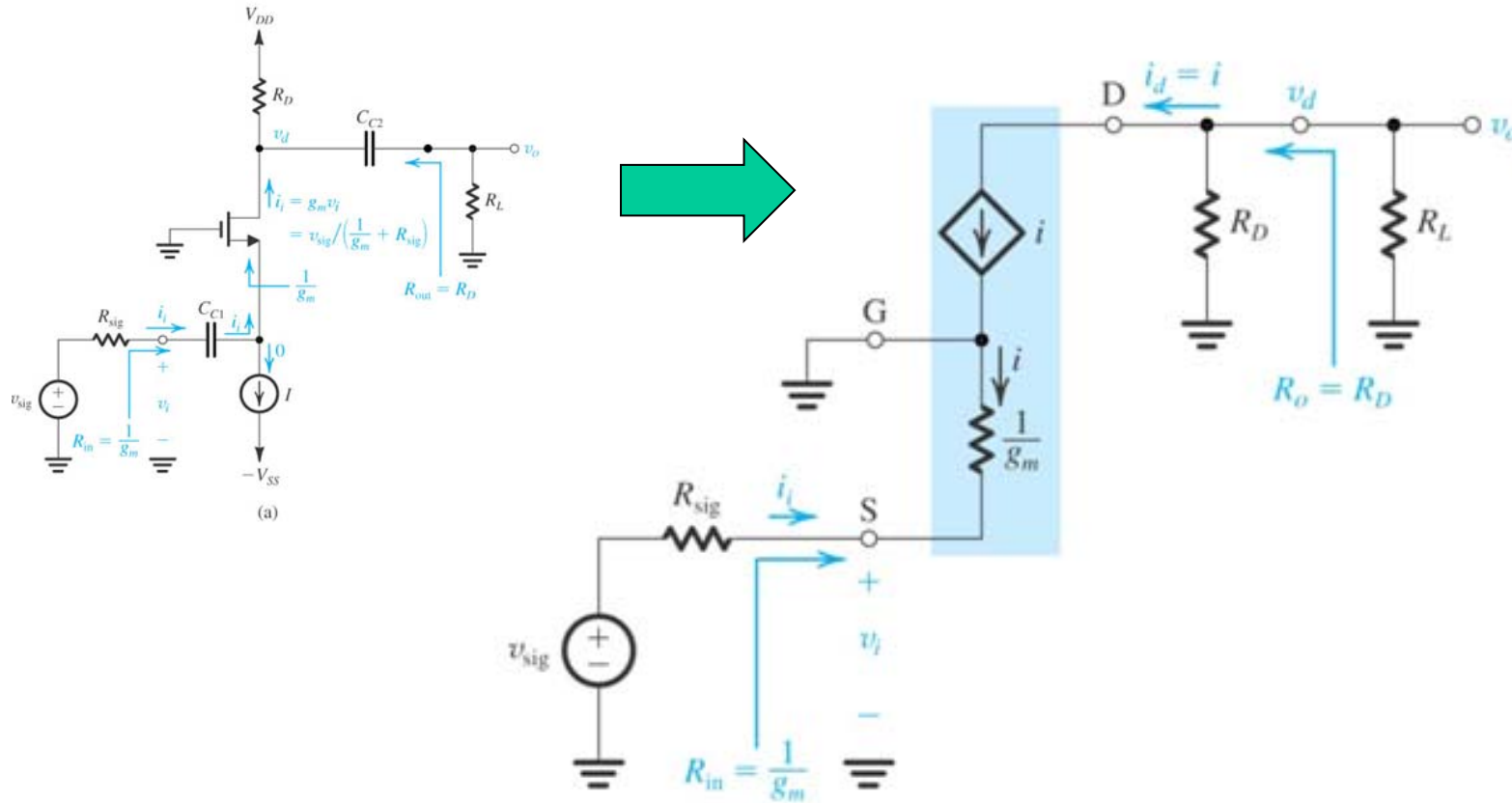
Single-Stage MOS Amplifiers

- ◆ Common Gate Amplifier (biasing w/ current source)



Single-Stage MOS Amplifiers

◆ Common Gate Amplifier



Equivalent circuit of the amplifier for small-signal analysis.

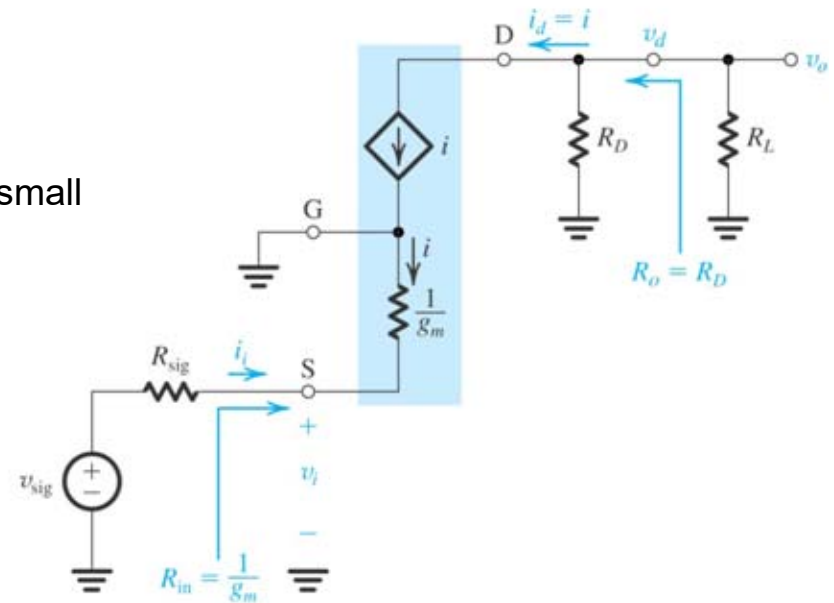
$$R_{in} = \frac{1}{g_m} \quad \text{Low input resistance}$$

$$v_i = v_{sig} \frac{R_{in}}{R_{in} + R_{sig}}$$

$$v_i = v_{sig} \frac{\frac{1}{g_m}}{\frac{1}{g_m} + R_{sig}} = v_{sig} \frac{1}{1 + g_m R_{sig}}$$

$$R_{sig} \ll \frac{1}{g_m} \quad \text{:to keep the loss in signal strength small}$$

$$i_i = \frac{v_i}{R_{in}} = \frac{v_i}{1/g_m} = g_m v_i$$

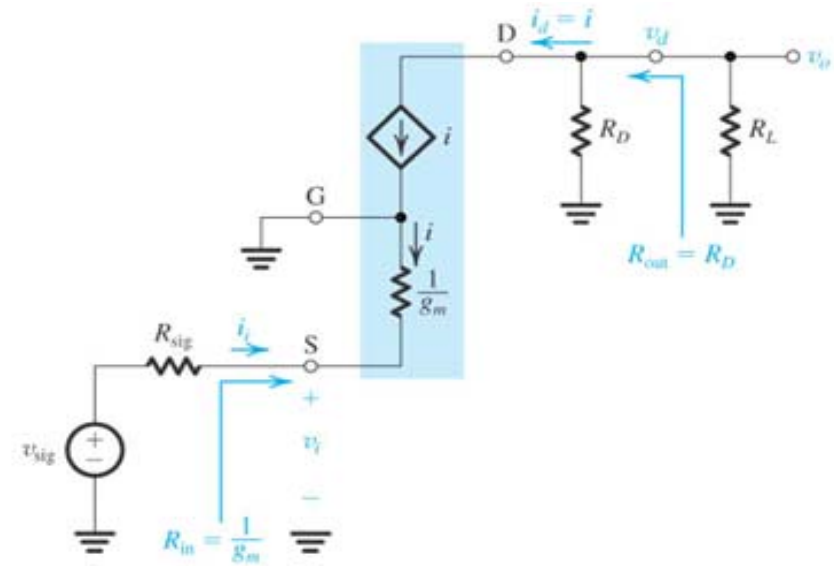


$$i_d = i = -i_i = -g_m v_i$$

$$v_o = v_d = -i_d (R_D \parallel R_L) = g_m (R_D \parallel R_L) v_i$$

$$A_v = g_m (R_D \parallel R_L)$$

$$A_{vo} = g_m R_D$$



$$G_v = \frac{R_{in}}{R_{in} + R_{sig}} A_v = \frac{1}{\frac{1}{g_m} + R_{sig}} A_v = \frac{A_v}{1 + g_m R_{sig}}$$

Relatively low gain compared to CS

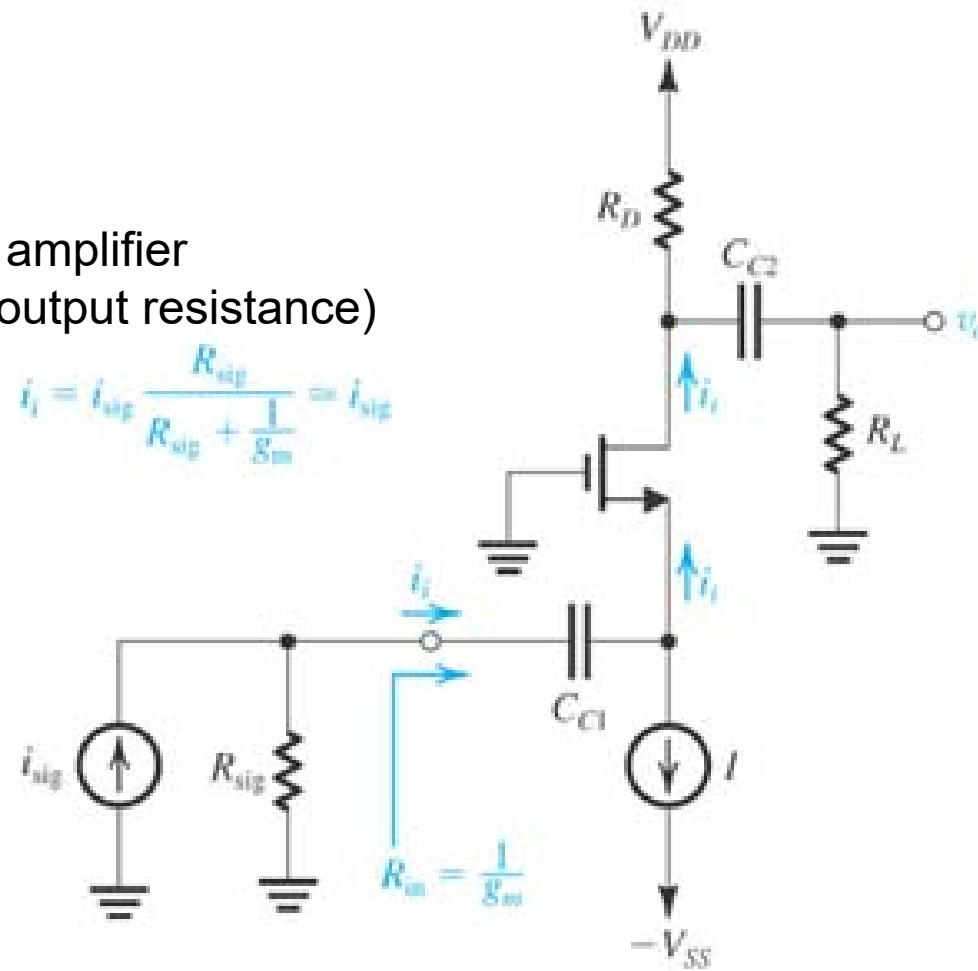
$$G_v = \frac{g_m (R_D \parallel R_L)}{1 + g_m R_{sig}}$$

$$R_{out} = R_o = R_D \quad (\text{by assuming } v_{sig} = 0)$$

$$i_i = i_{\text{sig}} \frac{R_{\text{sig}}}{R_{\text{in}} + R_{\text{sig}}} = i_{\text{sig}} \frac{R_{\text{sig}}}{R_{\text{sig}} + \frac{1}{g_m}} \quad \text{when } R_{\text{sig}} > \frac{1}{g_m}$$

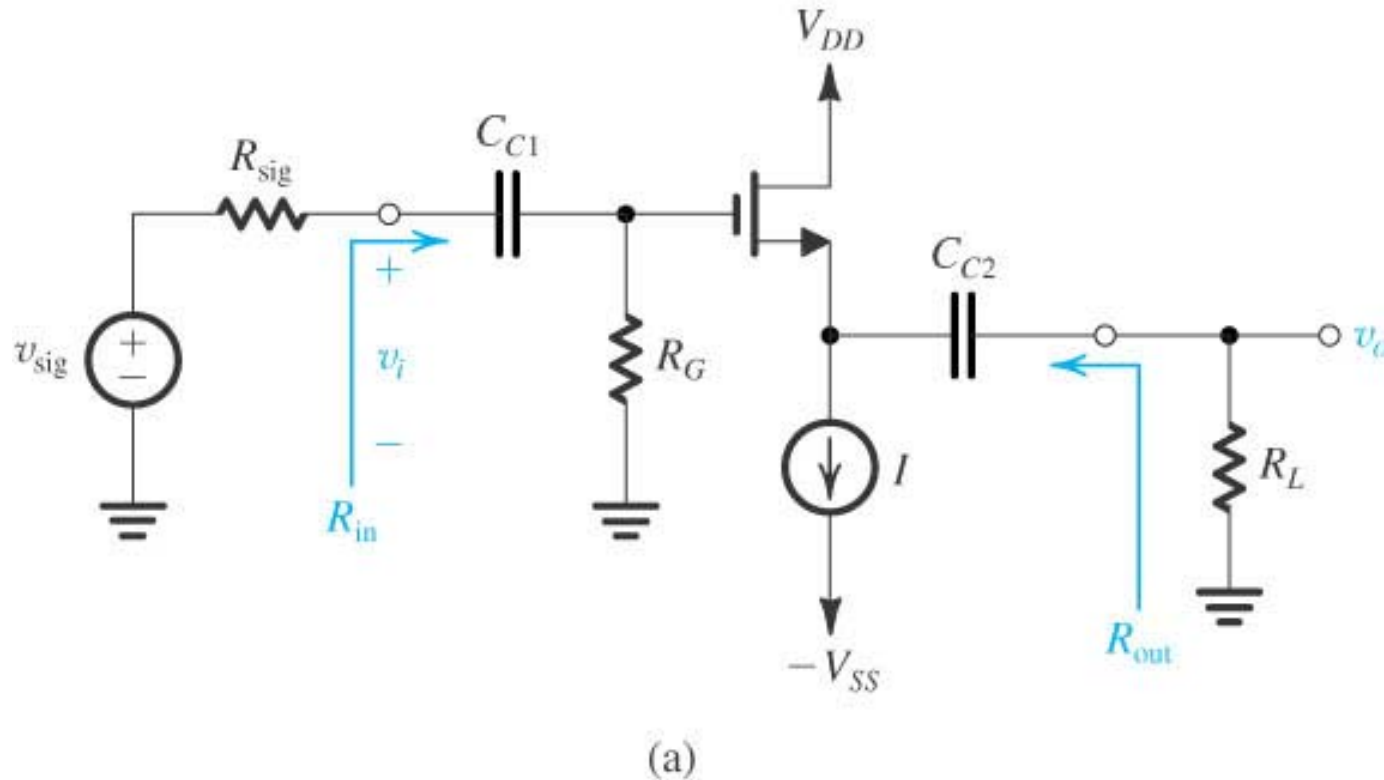
$$i_i \cong i_{\text{sig}}$$

Useful as a unity gain current amplifier
(small input resistance, large output resistance)



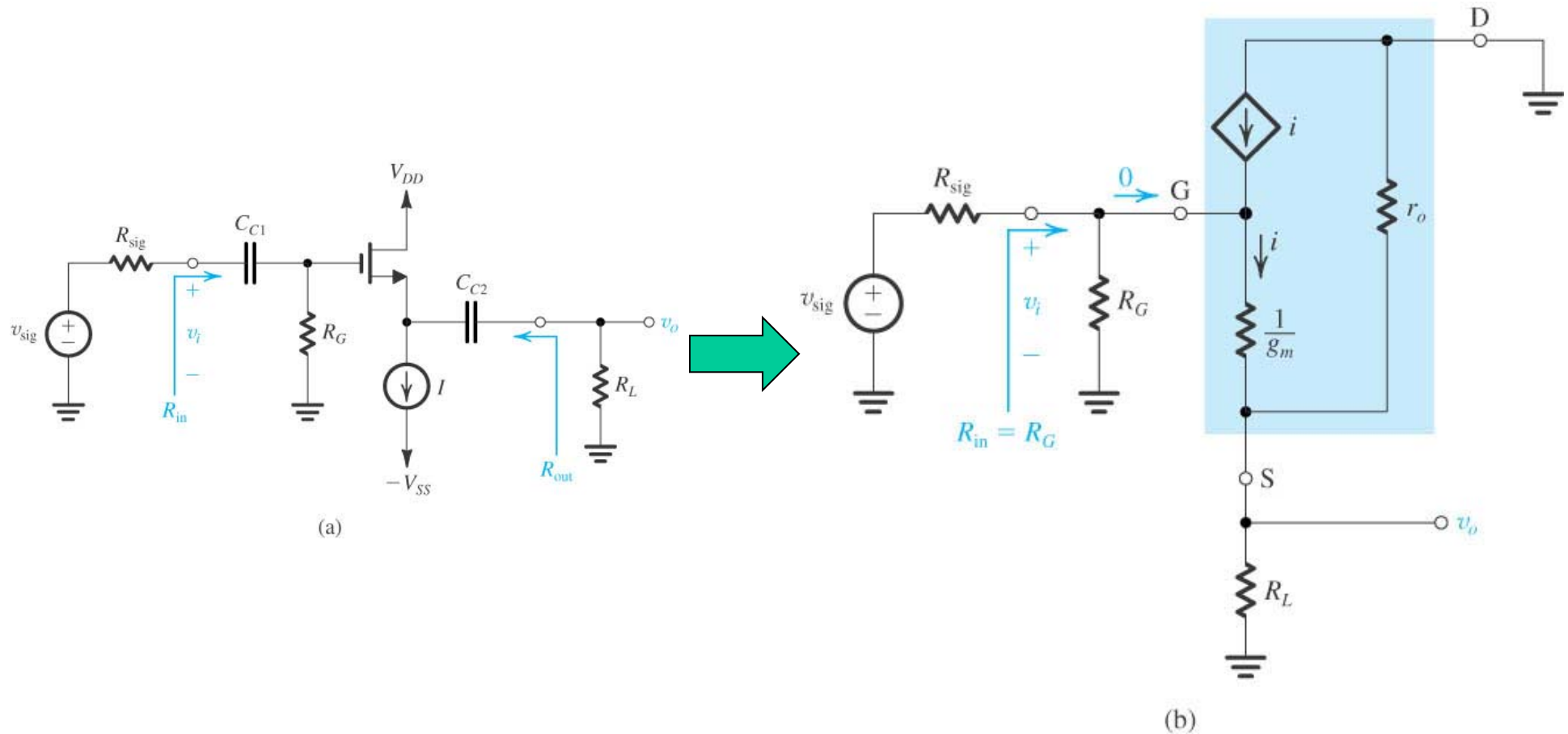
Single-Stage MOS Amplifiers

◆ Common Drain Amplifier (Source Follower)



Single-Stage MOS Amplifiers

◆ Source Follower



Equivalent circuit of the amplifier for small-signal analysis.

$$R_{in} = R_G$$

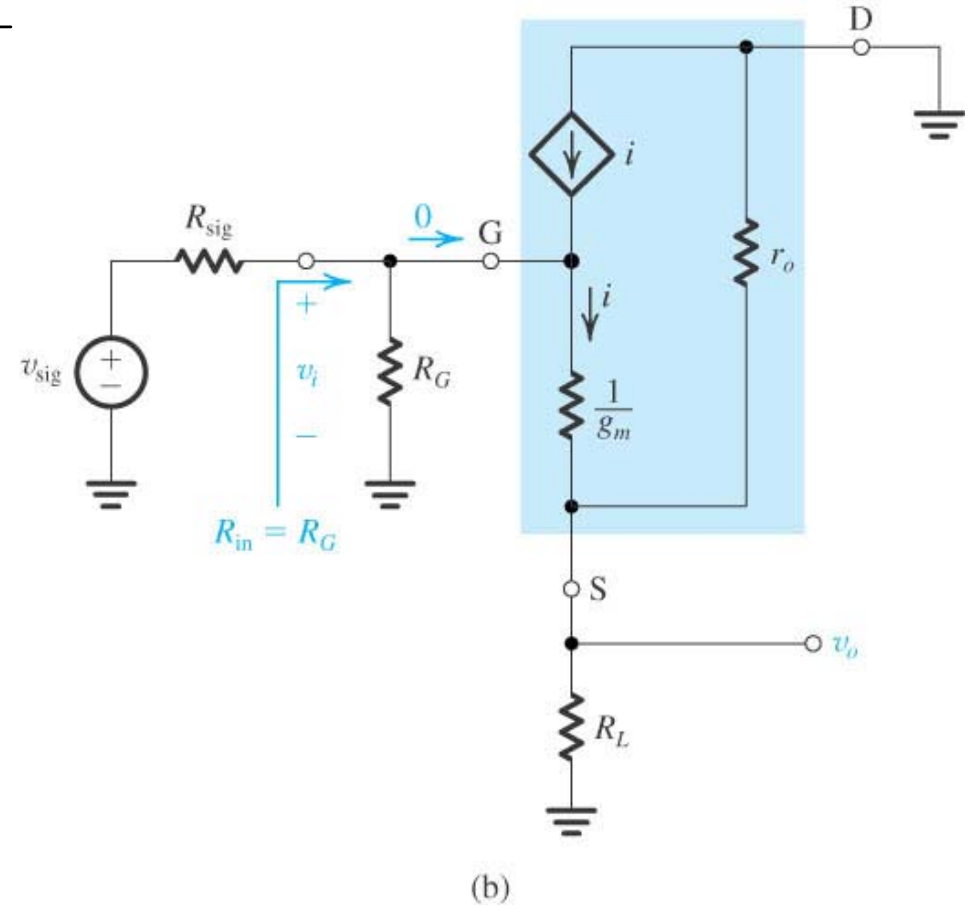
$$v_i = v_{sig} \frac{R_{in}}{R_{in} + R_{sig}} = v_{sig} \frac{R_G}{R_G + R_{sig}}$$

$$v_i \cong v_{sig}$$

$$v_o = v_i \frac{R_L \parallel r_o}{(R_L \parallel r_o) + \frac{1}{g_m}}$$

$$A_v = \frac{R_L \parallel r_o}{(R_L \parallel r_o) + \frac{1}{g_m}}$$

$$A_{vo} = \frac{r_o}{r_o + \frac{1}{g_m}} \sim 1$$

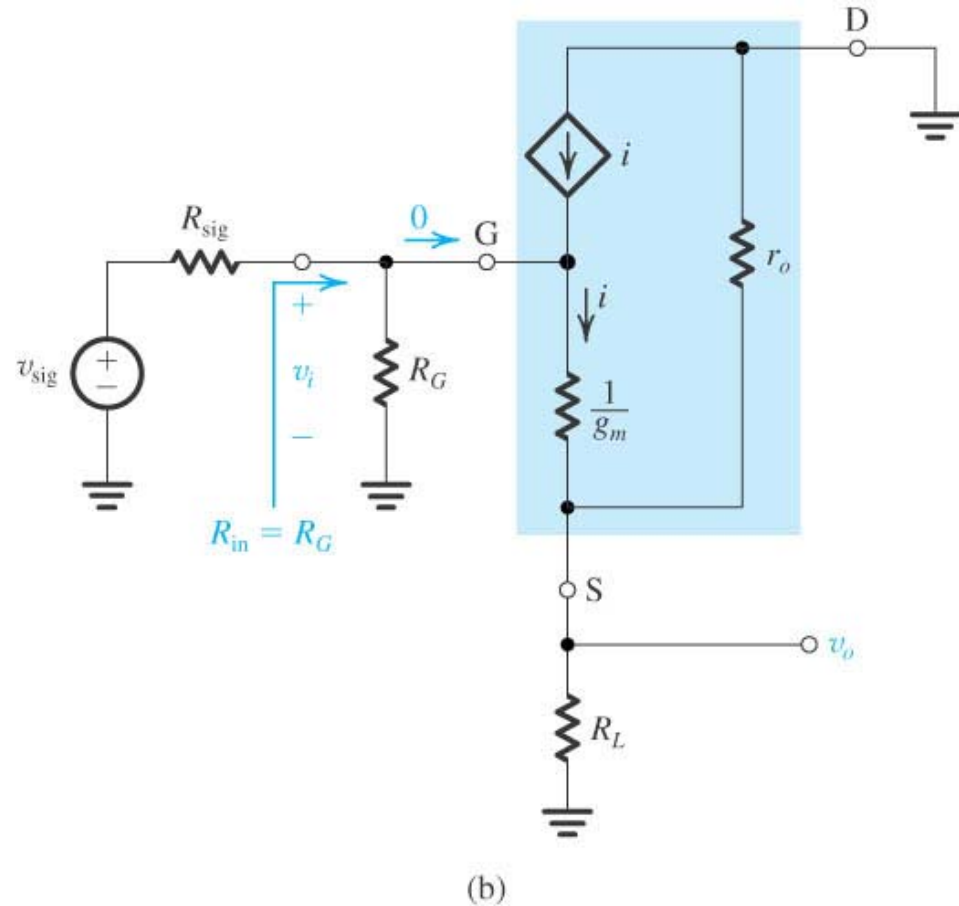


$$A_v \cong \frac{R_L}{R_L + \frac{1}{g_m}} \quad \text{When } r_o \gg R_L$$

$$G_v = \frac{R_G}{R_G + R_{\text{sig}}} \frac{R_L \parallel r_o}{(R_L \parallel r_o) + \frac{1}{g_m}}$$

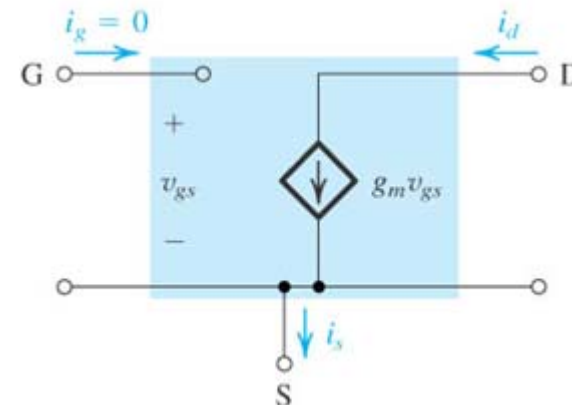
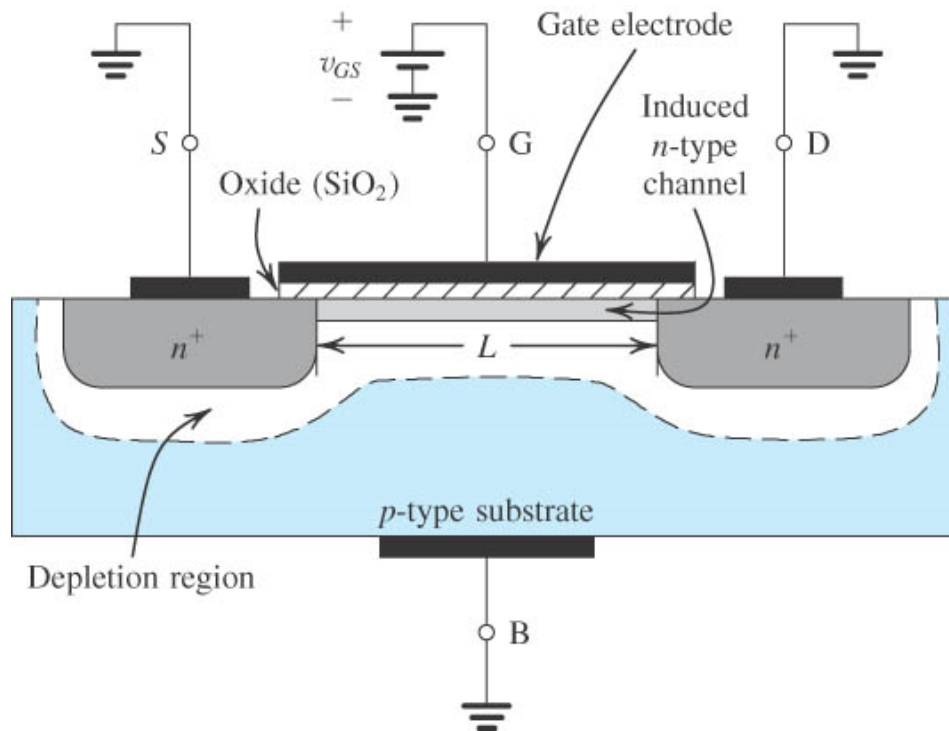
$$R_{\text{out}} = \frac{1}{g_m} \parallel r_o \quad (\text{by assuming } v_{\text{sig}} = 0)$$

$$R_{\text{out}} \cong \frac{1}{g_m} \quad \text{Gain: } \sim 1, \text{ high input resistance, low output resistance, voltage buffer}$$



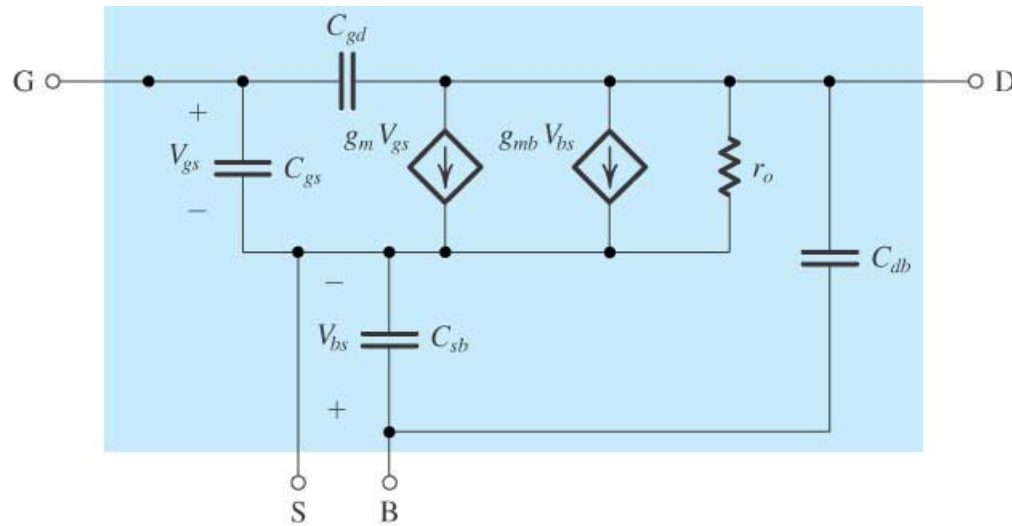
The MOSFET Internal Capacitance and High-Frequency Model

◆ MOSFET internal capacitance

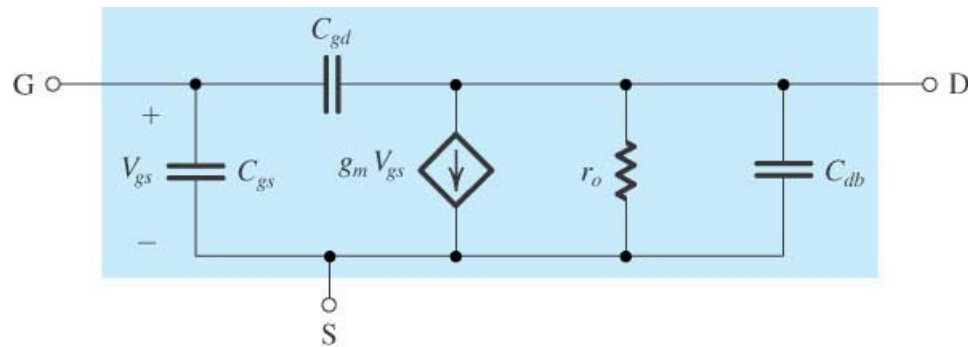


Why did we neglect the effect of internal capacitance in MOSFET until yet ?

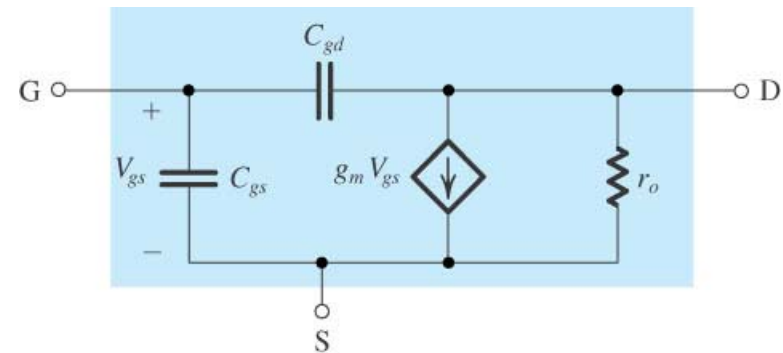
◆ High-frequency equivalent circuit model for MOSFET



(a)



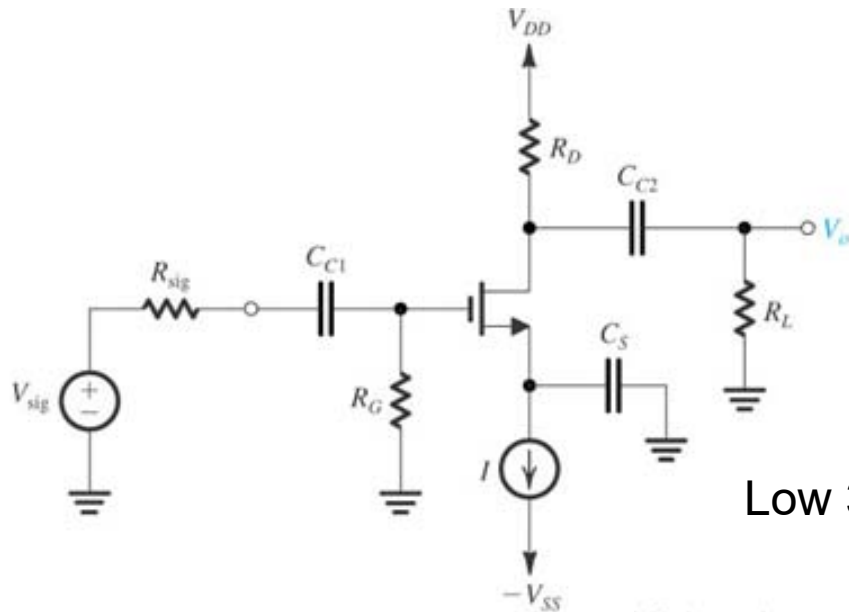
(b)



(c)

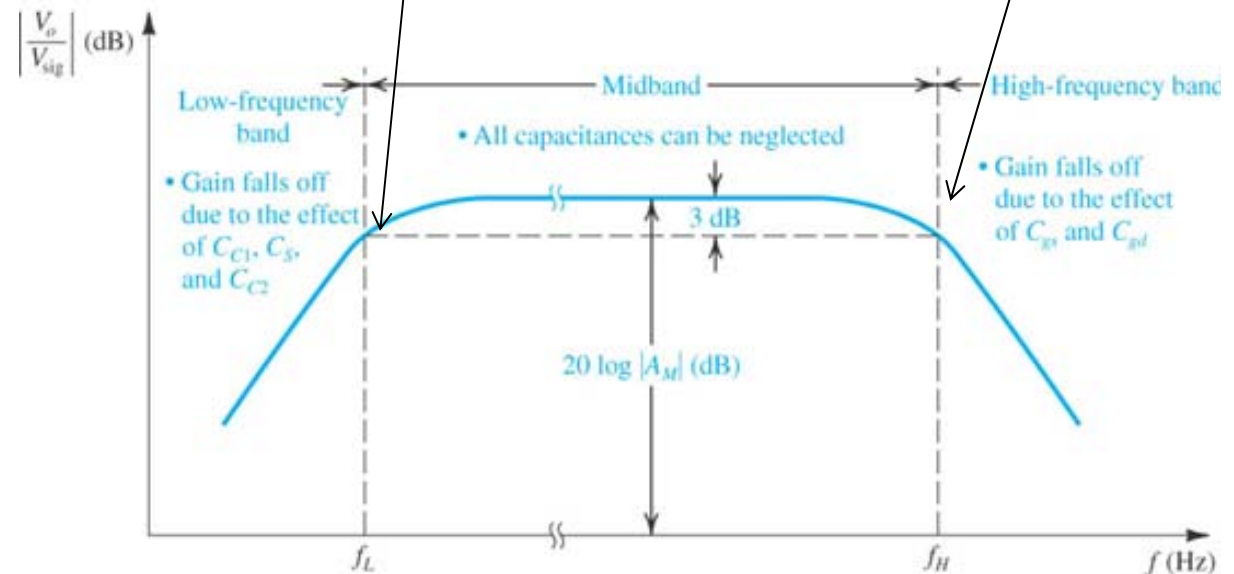
(a) High-frequency equivalent circuit model for the MOSFET. **(b)** The equivalent circuit for the case in which the source is connected to the substrate (body). **(c)** The equivalent circuit model of (b) with C_{db} neglected (to simplify analysis).

Frequency Response of the CS Amplifier



Low 3-dB frequency

High 3-dB frequency



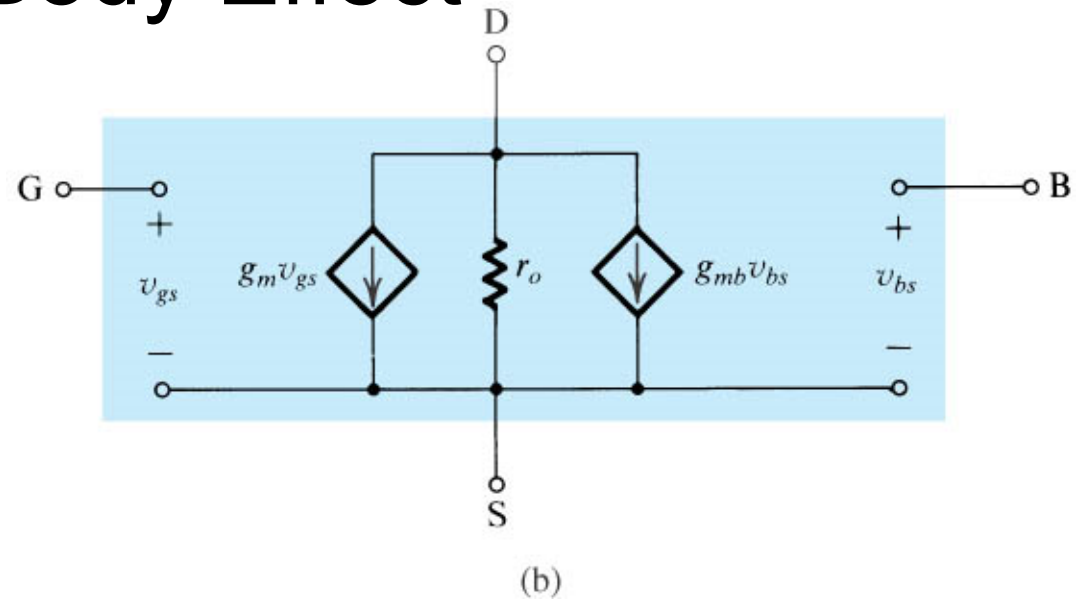
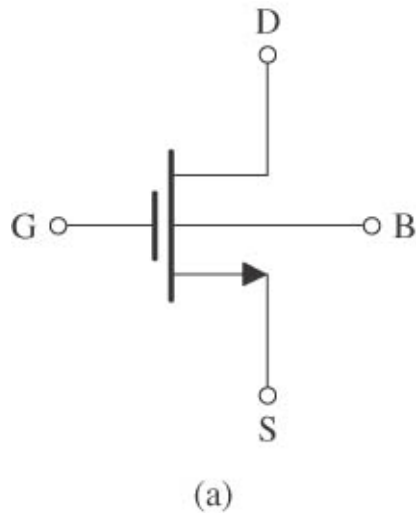
$$\mathbf{A}_M \equiv \frac{\mathbf{V}_o}{\mathbf{V}_{\text{sig}}} = \frac{\mathbf{R}_G}{\mathbf{R}_G + \mathbf{R}_{\text{sig}}} g_m (\mathbf{r}_o \parallel \mathbf{R}_D \parallel \mathbf{R}_L)$$

$$\mathbf{BW} \equiv f_H - f_L$$

$$\mathbf{BW} \cong f_H$$

$$\mathbf{GB} \equiv |\mathbf{A}_M| \mathbf{BW} \quad \text{Gain-Bandwidth product}$$

Body Effect



chi

$$g_{mb} \equiv \left. \frac{\partial i_D}{\partial v_{BS}} \right|_{\substack{v_{GS} = \text{constant} \\ v_{DS} = \text{constant}}} \quad (4.75)$$

$$g_{mb} \equiv \chi g_m \quad (4.76)$$

$$\chi \equiv \frac{\partial V_t}{\partial V_{SB}} = \frac{\gamma}{2\sqrt{2\phi_f + V_{SB}}} \quad (4.77)$$

Figure 4.41 Small-signal equivalent-circuit model of a MOSFET in which the source is not connected to the body.